

$$2\operatorname{tg}x + \operatorname{tg}2x = \operatorname{tg}4x$$

$$\operatorname{tg}x + \operatorname{tg}2x = \operatorname{tg}4x - \operatorname{tg}x$$

$$\frac{\sin x}{\cos x} + \frac{\sin 2x}{\cos 2x} = \frac{\sin 4x}{\cos 4x} - \frac{\sin x}{\cos x}$$

$$\frac{(\sin x \cdot \cos 2x + \sin 2x \cdot \cos x)}{\cos x \cos 2x} =$$

$$\frac{(\sin 4x \cdot \sin x - \cos 4x \cdot \cos x)}{\cos 4x \cos x}$$

$$\frac{\sin(3x)}{\cos x \cos 2x} = \frac{\sin 3x}{\cos 4x \cos x}$$

$$\sin 3x \left( \frac{1}{\cos x \cos 2x} - \frac{1}{\cos 4x \cos x} \right) = 0$$

$$x = \frac{\pi k}{3}$$

1 способ

$$\frac{(\cos 4x - \cos 2x)}{\cos x \cos 2x \cos 4x} = 0$$

$$\cos 4x - \cos 2x = 0$$

$$\cos 2x = -\frac{1}{2} \quad \cos 2x = 1$$

$$x = \frac{\pi}{3} + \pi k$$

$$x = \frac{2\pi}{3} + \pi k$$

$$x = \pi k$$

2 способ

$$\cos 4x - \cos 2x = 0$$

$$\cos a - \cos b = -2\sin \left( \frac{a+b}{2} \right) \sin \left( \frac{a-b}{2} \right)$$

$$\sin 3x = 0$$

$$\sin x = 0$$

$$x = \frac{\pi k}{3}$$

$$x = \pi k$$

Ответ  $x = \frac{\pi k}{3}$

